## **Collaborative Project – Functions and Their Graphs**

- 1. You are a plow truck operator for a snow removal company. Your weekly hours are based on weather conditions. You earn \$30 per hour for up to 40 hours and you are limited to at most 10 hours of overtime at one and one-half times your base pay rate.
  - **a.** Write and graph a piecewise-defined function E(x) that gives your earnings E for working x hours in one week.
  - b. Find your weekly earnings when you work 35 hours and when you work 50 hours.
  - **c.** Find and interpret the slope of each segment of the graph of E(x).
  - **d.** Find and interpret the intercepts of the graph of E(x).
  - e. You earn \$1515 in one week. How many hours did you work?
- 2. Your company orders a load of rock salt at a price of \$85 per ton. There is a delivery charge of \$95 and sales tax of 7%.
  - **a.** Explain what the function d(x) = 85x + 95 represents.
  - **b.** Write a function c(x) for the total cost of an amount of x dollars with a 7% tax added.
  - **c.** Find and interpret  $(d \circ c)(x)$  and  $(c \circ d)(x)$ .
  - d. There is no tax on the delivery fee. Find your company's total cost for 13 tons of salt.
- **3.** The graph of function *F* shows the approximate weekly revenues *y* of your company from last year. The graph of function *P* shows your company's projected weekly revenues *y* for this year. In each graph, *x* represents the week, with x = 0 corresponding to the first full week in October.



- **a.** Seasonal weather forecasts were used to create *P*. What can you conclude about these forecasts? Use the concepts of transformations of graphs to write *P* in terms of *F*.
- **b.** Determine the open intervals on which the function *P* is increasing, decreasing, or constant.
- c. Find the domain of each function.
- **4.** Your company purchases a truck for \$60,000 that is worth \$22,800 after 6 years. Find the average rate of change. Then write a linear function f(x) for the value f of the truck after x years. Find the inverse function  $f^{-1}(x)$  of f. Then find and interpret  $f^{-1}(35,200)$ .