

Project: Department of Defense The table shows the total numbers of Department of Defense personnel P (in thousands) from 1980 through 2010. (Source: U.S. Department of Defense)

| Year | Personnel, P | Year | Personnel, P |
|------|----------------|------|----------------|
| 1980 | 2051 | 1996 | 1472 |
| 1981 | 2083 | 1997 | 1439 |
| 1982 | 2109 | 1998 | 1407 |
| 1983 | 2123 | 1999 | 1386 |
| 1984 | 2138 | 2000 | 1384 |
| 1985 | 2151 | 2001 | 1385 |
| 1986 | 2169 | 2002 | 1414 |
| 1987 | 2174 | 2003 | 1434 |
| 1988 | 2138 | 2004 | 1427 |
| 1989 | 2130 | 2005 | 1389 |
| 1990 | 2044 | 2006 | 1385 |
| 1991 | 1986 | 2007 | 1380 |
| 1992 | 1807 | 2008 | 1402 |
| 1993 | 1705 | 2009 | 1419 |
| 1994 | 1610 | 2010 | 1431 |
| 1995 | 1518 | | |

(a) Use a graphing utility to plot the data. Let t represent the year, with $t = 0$ corresponding to 1980.

(b) A model that approximates the data is given by

$$P = \frac{9.6518t^2 - 244.743t + 2044.77}{0.0059t^2 - 0.131t + 1}$$

where P is the total number of personnel (in thousands) and t is the year, with $t = 0$ corresponding to 1980. Create a table showing the actual values of P and the values of P obtained using the model.

- (c) Does it appear that the model is a good fit for the data? Explain your reasoning.
- (d) Examine the scatter plot in part (a). Is there another type of model that can be used to model the data? Explain your reasoning.
- (e) Use the *regression* feature of a graphing utility to find the type of model described in part (d) for the data. Let t represent the year, with $t = 0$ corresponding to 1980.
- (f) Use a graphing utility to graph the original data and both the given rational model and the model that you found in part (e) in the same viewing window.
- (g) Use both models to predict the total personnel in 2018. Which model should be used to predict future values? Explain your reasoning.